

(October 26, 2018)

## *Corrections to Book\_28Aug2017.pdf*

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... to *Modern Analysis of Automorphic Forms, by Example*

These are pre-publication typos/corrections that appear in the on-line version of the book, [www.math.umn.edu/~garrett/m/v/Book\\_28Aug2017.pdf](http://www.math.umn.edu/~garrett/m/v/Book_28Aug2017.pdf) but almost entirely do *not* appear in the physical or electronic books published by CUP.

The page-number appearing on the page and the literal page-number of the PDF are identical in the 8.5x11 versions I have put and will put on-line.

Page 2 line 12, ‘explication’ should be ‘explication of’

Page 47 line -9, // should be /

Page 64 line -8, ‘direclty’ should be ‘directly’

Page 73 line -10,  $y^2$  should be  $y_2$

Page 80 line -9,  $t_\setminus = 0$  should be  $t_o \neq 0$

Page 89 line -9, in display,  $\ell$  should be  $r_\ell$

Page 100 line 9,  $\mathbb{J}_\ell^1/k^\times$  should be  $\mathbb{J}_\ell^1/\ell^\times$

Page 140/162 line 12,  $V_\ell$  should be  $V_\ell)$

Page 108 -15,  $k^\times$  should be  $k^\times$

Page 111 line 10, [3.5] should be [3.4]

Page 116 line 3,  $\chi(m)$  should be  $\chi(m) \cdot \varphi(g)$

Page 126 line 3,  $t^2$  should be  $t_2$

Page 135 line 2,  $\mathfrak{k}$  should be  $k$

Page 141 line -13, ‘immediate’ should be ‘immediately’

Page 141 line -13,  $\gamma$  should be  $\alpha$

Page 143 line 20, two superfluous )’s

Page 146 line 13,  $q$  should be  $\mathfrak{q}$

Page 154 line -9,  $q$  should be  $\mathfrak{q}$

Page 155 line 3,  $\int_{i\mathfrak{a}^*}$  should be  $\int_{i\mathfrak{q}^*}$

Page 163 line 13,  $j\mathfrak{g}$  should be  $j : \mathfrak{g}$

Page 168 line -8, ‘possibiities’ should be ‘possibilities’

Page 171 line 9,  $\mathfrak{sp}^*1, 1$  should be  $\mathfrak{sp}_{1,1}^*$

Page 172 line 2, ‘all  $\mathfrak{k}$ ’ should be ‘all in  $\mathfrak{k}$ ’

Page 183 line 19, ‘opern’ should be ‘open’

Page 186 line -10, ‘[9.E.2]yields’ should be ‘[9.E.2] yields’

Page 187 line 6,  $|_L^2$  should be  $|_{L^2}$

Page 199 line 5,  $\dot{\text{ch}}$  should be  $\text{ch}$  (without dot)

Page 205 line -18, ‘that that’ should be ‘that’

Page 214 line 17,  $\geq t$  should be  $\geq \tau$

Page 221 line 12,  $f(x, y)$  should be  $f(x, y))$

Page 222 line 16, ‘most’ should be ‘mostly’

Page 223 line 15,  $\mathfrak{n}_v = \mathfrak{n}_A =$  should be  $\mathfrak{n}_v =$

Page 227 line -10,  $C_c^\infty(\mathcal{G})$  should be  $C_c^\infty(G)$

Page 229 line -11, ‘irreducibles’ should be ‘irreducible’

Page 230 line 11, ‘corollaries *commutative*’ should be ‘corollaries about *commutative*’

Page 231 line 6,  $\in\in$  should be  $\in$

Page 235 line 6,  $\xi_{i'j''}$  should be  $\xi_{i'j'}$

Page 237 line -15, ‘[7.A]’ should be ‘[7.A.4]’

Page 240 line -11, ‘claim’ should be ‘claim.’

Page 251 line -5, ‘series formed’ should be ‘series’

Page 253 line 1,  $m_n$  should be  $m_r$

Page 253 line 7, ‘series formed’ should be ‘series’

Page 257 line 21,  $\lambda\lambda$  should be  $\lambda$

Page 259 line 9,  $\|\cdot\|_1$  should be  $|\cdot|_1$

Page 259 line 13,  $\|\cdot\|_1$  should be  $|\cdot|_1$

Page 259 line 13, ‘injects’ should be ‘maps’

Page 259 line 15, Delete the sentence ‘We identify  $V^1$  with its natural image inside  $V$ , noting that  $V^1$  has a finer topology than would be induced from  $V$ .’

Page 259 line 22, at the beginning of the proof, insert ‘First, let  $j$  be the continuous linear map  $j : V^1 \rightarrow V$  obtained by extending by continuity the identity map  $D \rightarrow D$ , with the

source being given the  $|\cdot|_1$  topology and the target being given the  $|\cdot|$  topology. We claim that  $j$  is an injection. By construction,  $\langle v, w \rangle_1 = \langle jv, Tw \rangle$  for  $v \in V^1$  and  $w \in D$ . For  $0 \neq v \in V^1$ , since  $D$  is dense in  $V^1$ , there exists  $w \in D$  such that  $\langle v, w \rangle_1 \neq 0$ . For that  $v$ ,

$$0 \neq \langle v, w \rangle_{V^1} = \langle jv, Tw \rangle$$

Thus,  $jv \neq 0$  for  $0 \neq v \in V^1$ , and  $j$  is indeed injective. We may identify  $V^1$  with its image in  $V$ , noting that  $V^1$  has a finer topology than that induced from  $V$ .

Page 272 line 7, ‘vanish at 0’ should be ‘vanish at  $\infty$ ’

Page 280 line 5, ‘Gårding’s theorem [14.6].’ should be ‘by smoothing of distributions [14.5].’

Page 281 line 18,  $(T^*)^*$  should be  $(T^*)^*$

Page 284 line -3,  $Tc$  should be  $Tx$

Page 284 line -15,  $Tc$  should be  $Tx$

Page 289 line -12,  $ToW_1$  should be  $\longrightarrow W_1$

Page 291 line -12,  $|f(T)$  should be  $|f(T)|$

Page 292 line 2, delete ‘lambar’

Page 299 line 6, replace ‘such that’ by ‘satisfies’

Page 300 line 11, in display,  $\int_{C_a}$  should be  $\int_{C_{a-\frac{1}{t}}}$

Page 301 lines 11-12, insert ‘cut off at height  $c$ ’

Page 306 line 10,  $\langle x_\alpha, x_\alpha^\theta \rangle = 1$  should be  $\langle x_\alpha, x_\alpha^\theta \rangle = -1$

Page 306 line 12,  $\Omega' = \sum$  should be  $\Omega' = -\sum$

Page 306 line 15 should read  $x_\beta x_\beta^\theta + x_\beta^\theta x_\beta = -2x_\beta^2 + 2x_\beta(x_\beta + x_\beta^\theta) + [x_\beta^\theta, x_\beta] \in -2x_\beta^2 + [x_\beta^\theta, x_\beta] + \mathfrak{k}$

Page 306 line 17 should have a sign flipped: it should be  $\Omega' = \sum_{\beta \in \Phi^N} 2x_\beta^2 - [x_\beta^\theta, x_\beta]$

Page 306 line -1,  $-\sum$  should be  $\sum$ , that is, flip the sign

Page 307 line 2, a sign flip:  $-\sum_{\beta \in \Phi^N} [x_\beta^\theta, x_\beta]$  should be  $\sum_{\beta \in \Phi^N} [x_\beta^\theta, x_\beta]$

Page 307 line 6,  $T = -\sum$  should be  $T = \sum$ , that is, a single sign flip

Page 316 line 18, ‘so Friedrichs’ should be ‘so has Friedrichs’

Page 316 line -5, ‘some  $\theta$  the’ should be ‘some  $\theta$  in’

Page 332 line 14,  $S^\#x = y$  should be  $S^\#x = (t^* \circ (j^* \circ c))y$

Page 332 line 15, delete display

Page 332 line 16, delete ‘and’

Page 336 line -2, delete ‘ $\infty >$ ’

Page 336 line -1,  $\gg$  should be  $\ll$

Page 345 line 5, should be  $\rho^* : C_c^\infty(\mathbb{R}^m)^* \rightarrow C_c^\infty(\mathbb{R}^{m+n})^*$

Page 357 line 12, should begin  $((1 - \Delta)f)(F) =$ , that is, add left parenthesis

Page 358 line 13,  $H^{ell}$  should be  $H^\ell$

Page 358 line 13, ‘show that a’ should be ‘show that’

Page 366 line 12, ‘incompatibly’ should be ‘incompatible’

Page 366 line 7,  $u_w^z$  should be  $u_{w,z}$

Page 366 line 9,  $u_w^z$  should be  $u_{w,z}$

Page 366 line -6,  $c_{1-s}a^s$  should be  $c_{1-s}a^s$

Page 369 line 1, ‘ $e^{\pm 2\pi y}$  alone’ should be  $e^{2\pi y}$  alone’

Page 370 line 12, ‘Given  $f$ ’ should be ‘Let  $f$  be’

Page 375 line 2, ‘nor merely’ should be ‘not merely’

Page 380 line -14, in display,  $d_k(x_k - y_k)$  should be  $d_k(x_k, y_k)$ , twice

Page 384 line 5,  $x \in k$  should be  $x \in \mathbb{C}$

Page 384 line 6, ‘over  $k$ ’ should be ‘over  $\mathbb{C}$ ’

Page 384 line 9,  $x_o \in k$  should be  $x_o \in \mathbb{C}$

Page 384 line -20,  $k \rightarrow V$  should be  $\mathbb{C} \rightarrow V$

Page 384 line -19, ‘in  $k$ ’ should be ‘in  $\mathbb{C}$ ’

Page 384 line -19,  $\alpha \in k$  should be  $\alpha \in \mathbb{C}$

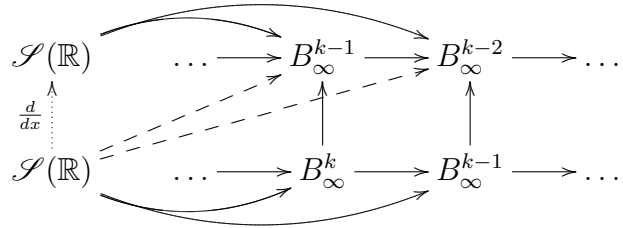
Page 387 line 2 (lower line of diagram)  $C^{k-1}(K_n)$  should be  $C^k(K_n)$

Page 391, both the two displays should express  $\mathcal{S}$  as diagonal limits of  $B_n^k$ 's. One way is to modify things to

*Proof:* This is structurally the same as before: letting  $B_\infty^k$  be the space of  $C^k$  functions of rapid decay, from the commutative diagram

$$\begin{array}{ccccccc}
 & & \curvearrowright & & \curvearrowright & & \\
 \mathcal{S}(\mathbb{R}) & & \longrightarrow & B_\infty^{k-1} & \longrightarrow & B_\infty^{k-2} & \longrightarrow \dots \\
 & & & \uparrow \frac{d}{dx} & & \uparrow \frac{d}{dx} & \\
 \mathcal{S}(\mathbb{R}) & & \longrightarrow & B_\infty^k & \longrightarrow & B_\infty^{k-1} & \longrightarrow \dots \\
 & & \curvearrowleft & & \curvearrowleft & & 
 \end{array}$$

composing the projections with  $d/dx$  to give (dashed) induced maps from  $\mathcal{S}(\mathbb{R})$  to the limitands, inducing a unique (dotted) continuous linear map to the limit:



as desired.

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Page 402 line 10, 'vis' should be 'via'

Page 412 line 3, 'notion *smoothness*' should be 'notion of *smoothness*'

Page 412 line -10, 'transforms are' should be 'transforms that are'

Page 418 line -5, in display, insert  $\implies$ , so that it reads (in part) ' $|x - x_o| < \delta \implies \sup \dots$ '

Page 421 line 12, 'uniqueness:' should be 'uniqueness.'

Page 453 line 7, 'instances general' should be 'instances of general'

Page 464 lines -3, -4, needless linebreak

Page 467 lines -12, -13, needless linebreak

Page 473 line -18, 'Asmptotic' should be 'Asymptotic'

Page 479 between lines 13 and 14, insert reference [Shalika 1974], J.A. Shalika, *The multiplicity one theorem for  $GL_n$* , Ann. of Math. **100** (1974), 171-193.