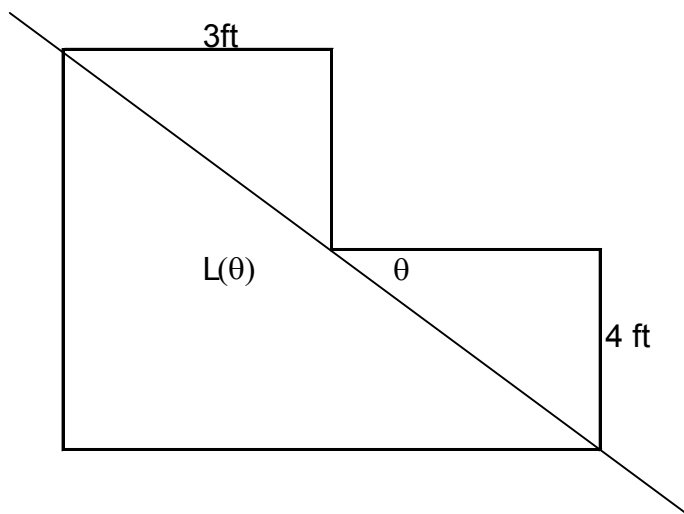


**ALTERNATIVE SOLUTION**

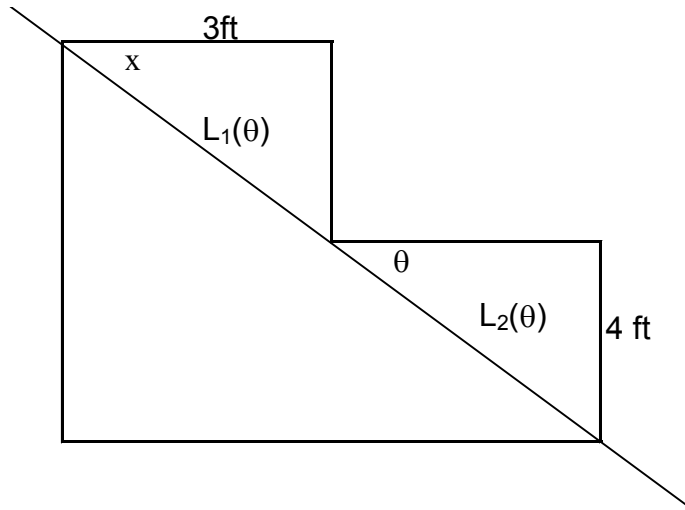
Author: Michael Sullivan  
Text: Precalculus, sixth edition  
Section: 5.6– Phase Shift; Sinusoidal Curve Fitting  
Pg.: 369  
Question: 5.6#35a

Show that the length  $L$  of the ladder as a function of the angle  $\theta$  is

$$L(\theta) = 3\sec \theta + 4\csc \theta$$



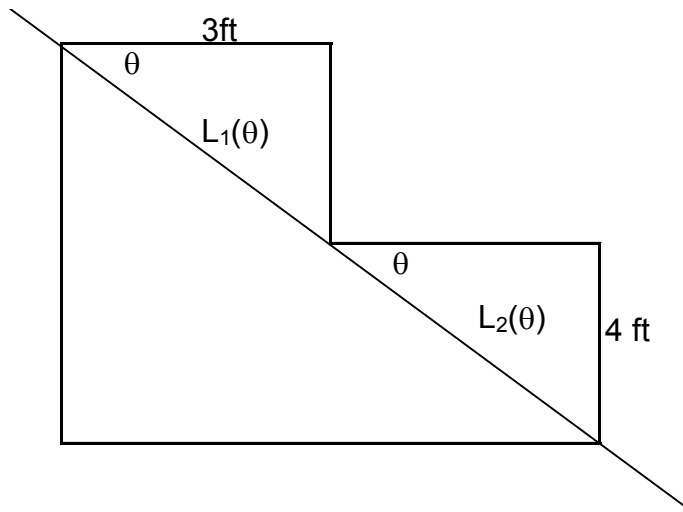
First, split  $L(\theta)$  into  $L_1(\theta)$  and  $L_2(\theta)$



$$\sin\theta = 4\text{ft} / L_2(\theta)$$

$$\text{Therefore, } L_2(\theta) = 4\text{ft} / \sin\theta$$

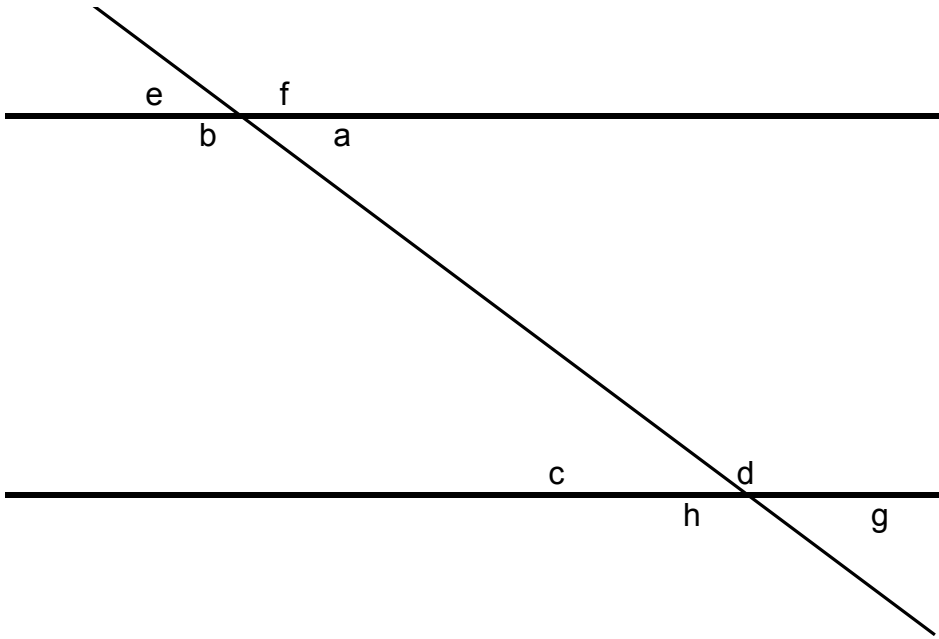
Then, you can automatically say that  $x = \theta$



This is because if two parallel lines are cut by a transversal, the corresponding angles are equal, alternate interior angles are equal, and alternate exterior angles are equal.<sup>1</sup>

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<sup>1</sup> Michael Serra, *Discovering Geometry: An Inductive Approach*, copyright 1997 Michael Serra, pg. 179



$$a = e = c = g \quad \text{and} \quad f = b = d = h$$

Now you can determine that

$$\cos \theta = 3 \text{ ft} / L_1(\theta)$$

$$\text{Therefore, } L_1(\theta) = 3 \text{ ft} / \cos \theta$$

$$L(\theta) = L_1(\theta) + L_2(\theta) = (3 \text{ ft} / \cos \theta) + (4 \text{ ft} / \sin \theta) = 3 \sec \theta + 4 \csc \theta$$