

# Financial Mathematics

## Principal component analysis

0035-1.

Let  $e_1, e_2, e_3$  be the standard basis of  $\mathbb{R}^{1 \times 3}$ ,

$$\text{viz.,} \quad e_1 := [1 \quad 0 \quad 0],$$

$$e_2 := [0 \quad 1 \quad 0],$$

$$e_3 := [0 \quad 0 \quad 1].$$

a. Let  $v_1 := [2 \quad 4 \quad -2],$

Let  $v_2 := [1 \quad -1 \quad -1].$

Find a rotation matrix  $R$

and scalars  $c_1, c_2 \in \mathbb{R}$

such that  $c_1 e_1 R = v_1$  and  $c_2 e_2 R = v_2.$

b. Find a rotation matrix  $L$

such that  $v_1 L \in \mathbb{R}e_1$  and  $v_2 L \in \mathbb{R}e_2.$

0035-2. Let  $M := \begin{bmatrix} 1 & 2 & 0 \\ 2 & 0 & 2 \end{bmatrix}$ .

Find rotation matrices

$$K \in \mathbb{R}^{2 \times 2} \quad \text{and} \quad L \in \mathbb{R}^{3 \times 3}$$

s.t.  $KML$  is “diagonal”.