VERSION B

MATH 1271 Fall 2011, Midterm #2 Handout date: Thursday 10 November 2011

PRINT YOUR NAME:

50 LUTIONS

PRINT YOUR TA'S NAME:

WHAT SECTION ARE YOU IN?

Closed book, closed notes, no calculators/PDAs; no reference materials of any kind. Turn off all handheld devices, including cell phones.

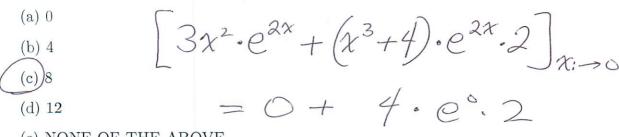
Show work; a correct answer, by itself, may be insufficient for credit. Arithmetic need not be simplified, unless the problem requests it.

I understand the above, and I understand that cheating has severe consequences, from a failing grade to expulsion.

SIGN YOUR NAME:

## I. Multiple choice

A. (5 pts) (no partial credit) Find the slope of the tangent line to  $y=(x^3+4)e^{2x}$  at the point (0,4).



(e) NONE OF THE ABOVE

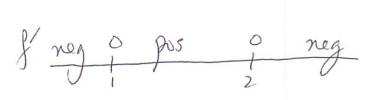
B. (5 pts) (no partial credit) Compute  $\lim_{x\to 0} \left[ \frac{\sin^2 x}{4x^3 + 2x^2} \right]$ .

- (b) 1/4
- (c) 2
- (d) 1
- (e) NONE OF THE ABOVE

C. (5 pts) (no partial credit) Suppose  $f'(x) = -x^2 + 3x - 2$ . At most one of the following statements is true. If one is, circle it. Otherwise, circle "NONE OF THE ABOVE".

- (a) f is increasing on  $(-\infty, -2]$ , decreasing on [-2, -1] and increasing on  $[-1, \infty)$ .
- (b) f is decreasing on  $(-\infty, -2]$ , increasing on [-2, -1] and decreasing on  $[-1, \infty)$ .
- (c) f is increasing on  $(-\infty, 1]$ , decreasing on [1, 2] and increasing on  $[2, \infty)$ .
- (d) If is decreasing on  $(-\infty, 1]$ , increasing on [1, 2] and decreasing on  $[2, \infty)$ .
  - (e) NONE OF THE ABOVE

$$f(x) = -(x^2 - 3x + 2)$$
  
= -(x-1)(x-2)



D. (5 pts) (no partial credit) Find the logarithmic derivative of  $x^2 + 3x - 8$  w.r.t. x.

(a) 
$$\frac{x^2 + 3x - 8}{2x + 3}$$

(b) 
$$\frac{2x+3}{x^2+3x-8}$$

- (c)  $(\ln(x^2)) + 3(\ln x) (\ln 8)$
- (d) ln(2x+3)
- (e) NONE OF THE ABOVE

E. (5 pts) (no partial credit) Find the logarithmic derivative of  $(2 + \sin x)^x$  w.r.t. x.

(a) 
$$[(2 + \sin x)^x] \left[ (\ln(2 + \sin x)) + \left( \frac{x \cos x}{2 + \sin x} \right) \right]$$

$$(b)(\ln(2+\sin x)) + \left(\frac{x\cos x}{2+\sin x}\right)$$

- (c)  $\ln(\cos x)$
- (d)  $\cos x$
- (e) NONE OF THE ABOVE
- de [x (ln (2+ pin x))]

F. (5 pts) (no partial credit) Find the derivative of  $(2 + \sin x)^x$  w.r.t. x.

$$(a)[(2+\sin x)^x]\left[(\ln(2+\sin x))+\left(\frac{x\cos x}{2+\sin x}\right)\right]$$

- (b)  $(\ln(2+\sin x)) + \left(\frac{x\cos x}{2+\sin x}\right)$
- (c)  $\ln(\cos x)$
- (d)  $\cos x$
- (e) NONE OF THE ABOVE

II. True or false (no partial credit):
a. (5 pts) If f and g are differentiable, then $\frac{d}{dx}[(f(x))(g(x))] = [f'(x)][g'(x)].$
b. (5 pts) If $f' > 0$ on an interval $I$ , then $f$ is increasing on $I$ .
c. (5 pts) If $f'(3) = 0$ and $f''(3) > 0$ , then f has a local maximum at 3.
V
d. (5 pts) Every local extremum occurs at a critical number.
e. (5 pts) Every global extremum occurs at a critical number.
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THE BOTTOM OF THIS PAGE IS FOR TOTALING SCORES PLEASE DO NOT WRITE BELOW THE LINE
VERSION B
I. A,B,C
I. D,E,F
II. a,b,c,d,e
III. 1.
III. 2.
III. 3,4.

III. 5.

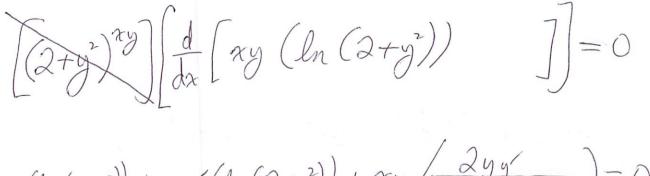
III. Computations. Show work. Unless otherwise specified, answers must be exactly correct, but can be left in any form easily calculated on a standard calculator.

1. (10 pts) Compute 
$$\frac{d}{dx} \left[ \frac{2x^3 - 8}{\arctan x} + xe^{\sin x} \right]$$

$$\frac{\left(\arctan x\right)\left(6x^{2}\right)-\left(2x^{3}-8\right)\left(\frac{1}{1+x^{2}}\right)}{\left(\arctan x\right)^{2}}+$$

$$\left(e^{\sin x}\right) + x\left(e^{\sin x}\right)\left(\cos x\right)$$

2. (10 pts) Using implicit differentiation (and logarithmic differentiation), find y' = dy/dx, assuming that  $(2 + y^2)^{xy} = 9$ .



$$y(ln(2+y^2)) + xy'(ln(2+y^2)) + xy(\frac{2yy'}{2+y^2}) = 0$$

$$y' = \frac{-y \left( \ln (2+y^2) \right)}{x \left( \ln (2+y^2) \right) + \frac{2xy^2}{2+y^2}}$$

3. (5 pts) Suppose f is 1-1 and  $g = f^{-1}$  is the inverse of f. Suppose f(3) = 4 and f'(3) = 64. Compute g(4) and g'(4).

$$g(4) = 3$$
 $g'(4) = \frac{1}{64}$ 

4. (10 pts) Find the maximal intervals of increase and decrease for  $f(x) = x^3 - 6x^2 + 5$ .

$$f'(x) = 3x^{2} - 12x$$

$$= 3x(x-4)$$

fis increasing on 
$$[-0, 0]$$
decreasing on  $[0, 4]$ 
increasing on  $[4, \infty)$ 

5. (10 pts) Among all pairs of positive numbers x and y such that xy = 100, find the global maximum value of x + 4y, provided it exists. Then find the global minimum value, provided it exists. (NOTE: If the global maximum value does not exist, you need to state that clearly to receive full credit. If it does exist, for full credit, you'll need to compute x + 4y; computing x and/or y alone is insufficient. These same comments apply to the global minimum value.)