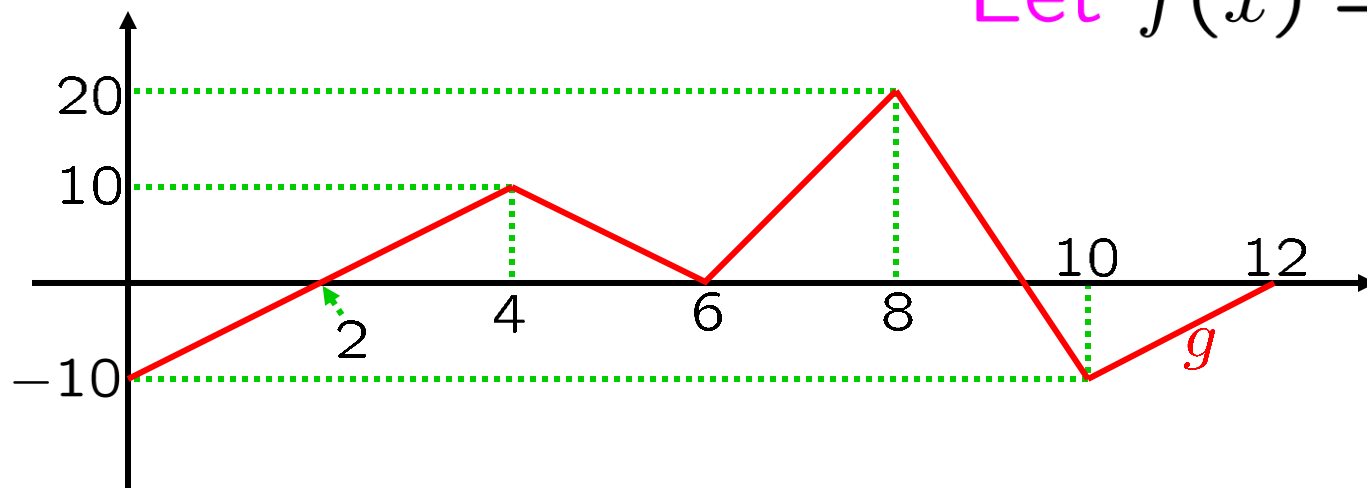


CALCULUS
The Fundamental Theorems of Calculus,
problems
NEW

0620-1. The graph of g is shown below.

NEW

Let $f(x) = \int_0^x g(t) dt$.



- Compute $f(12)$.
- Find the maximal intervals of increase and decrease for f .
- At what numbers does f have a local max and local min?
- Find the maximal intervals of concavity for f .
- What are the points of inflection for f ?

0620-2. Let $f(x) = \int_e^x t^5 - t^2 dt$.

- Compute a (polynomial) formula for $f(x)$.
- Compute a (polynomial) formula for $f'(x)$.

0620-3. Let $f(x) = \int_0^x e^{-2s^2} ds$.

- Sketch $y = e^{-2s^2}$, then choose some number on the s -axis, label it as x , and shade in a region under the graph whose area is $f(x)$.
- Compute a formula for $f'(x)$.

NEW 0620-4. Compute $\frac{d}{dx} \int_{\pi}^x \tan(q^6) dq.$

NEW 0620-5. Compute $\frac{d}{dx} \int_x^{\pi} \tan(q^6) dq.$

NEW 0620-6. Compute $\frac{d}{dx} \int_{\pi}^{x^3} \tan(q^6) dq.$

NEW 0620-7. Compute $\frac{d}{dx} \int_{\pi}^{x^4} \tan(q^6) dq.$

NEW 0620-8. Compute $\frac{d}{dx} \int_{x^3}^{\pi} \tan(q^6) dq.$

NEW 0620-9. Compute $\frac{d}{dx} \int_{x^3}^{x^4} \tan(q^6) dq.$

0620-10. Compute $\frac{d}{dr} \int_{-2 \sin 1}^{e^5 + e^4} e^{w^4 + 3w^3} dw.$

0620-11. Compute $\frac{d}{dt} \int_{-e^3}^{5+t^4} \arctan(w^2) dw.$

0620-12. Compute $\frac{d}{dt} \int_{-t^4-4}^0 \ln(2 + \sin x) dx.$

0620-13. Evaluate $\int_2^3 \left(\sqrt{x^3} + \frac{1}{x^2} \right) dx.$

0620-14. Evaluate $\int_1^4 \frac{7x^4 - 2x^2 + 3x + 8}{\sqrt[3]{x}} dx.$

0620-15. Evaluate $\int_{\pi/4}^{\pi/3} (e \sin t - 6 \cos t) dt.$

0620-16. Evaluate $\int_{\pi/4}^{\pi/3} (\csc^2 t) dt.$

0620-17. Evaluate $\int_0^1 \frac{1}{\sqrt{1 - (1 - (t/2))^2}} dt.$

0620-18. Evaluate $\int_{-1}^4 (x - |x|) dx.$

0620-19. Evaluate $\lim_{n \rightarrow \infty} \frac{2}{n} \left[\sum_{j=1}^n \left(1 + \frac{2j}{n} - \frac{1}{n} \right)^3 \right],$

by converting to a definite integral, and then using the Fundamental Theorem of Calculus.

0620-20. Evaluate $\lim_{n \rightarrow \infty} \frac{5}{n} \left[\sum_{j=0}^{n-1} \left(-2 + \frac{5j}{n} \right)^7 \right],$

by converting to a definite integral, and then using the Fundamental Theorem of Calculus.

0620-21. Evaluate $\lim_{n \rightarrow \infty} \frac{\pi}{2n} \left[\sum_{j=1}^n \sec^2 \left(-\frac{\pi}{4} + \frac{\pi j}{2n} \right) \right],$

by converting to a definite integral, and then using the Fundamental Theorem of Calculus.

0620-22. Water starts pouring from a tank.

NEW

After t minutes, the rate of flow, out of the tank is $3 + 2t^4$ gallons per minute.

How many gallons pour out between 7 and 8 minutes after the start?

0620-23. A model rocket is launched and starts climbing. After t seconds, its altitude is

NEW

increasing at $3 + 2t^4$ feet/second. How much does its altitude increase between 7 and 8 seconds after launch?

0620-24. At x ounces, the marginal cost of production for certain liquid is $3 + 2x^4$ dollars per ounce. How much does it cost to increase production from 7 to 8 ounces?

NEW



0620-25. A rope lies along a number line, between 0 and 100. The weight density of the rope at x is $3 + 2x^4$ pounds per inch. **How much** does the portion of the rope $x = 7$ and $x = 8$ weigh?

0620-26. By definition, **if** a force of F is applied to a particle over a distance s , **then** the **work** done is Fs . A 30 foot rope hangs from the top of a wall, and its density is 6 ounces per foot. We pull the rope up over the wall. Each particle of rope is acted on by a force equal to its weight, until it reaches the top of the wall (after which it simply coils up on the roof, which involves **no** work). **How much** work is done in pulling the rope up?

0620-27. By definition, **if** a force of F is applied to a particle over a distance s , **then** the **work** done is Fs . A certain object is lying on a frictionless horizontal number line, attached to a horizontal spring, which, in turn, is attached to a vertical wall. The wall crosses the number line at -2 , and the object is positioned on the number line at 0 . We pull the object from 0 to 8 . **Assume** that the spring pulls back with a force of $3x$, when the object is positioned at x . **Compute** the total work done by the spring.

