

**MATH 8307**  
**Additional Problems for Homework Assignment #3**  
**Due 02/14**  
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1. Show that  $\mathbf{CP}^n$  and  $\mathbf{S}^{2n} \vee \mathbf{S}^{2n-2} \vee \dots \vee \mathbf{S}^2$  have the same homology and cohomology groups, but these spaces aren't homotopy equivalent.
2. Let  $X$  be the topological space obtained from  $\mathbf{S}^m \times \mathbf{S}^m$  by identifying the points  $(x, x_0)$  and  $(x_0, x)$  for all  $x$  in  $\mathbf{S}^m$ . Compute the cohomology ring of  $X$  with  $\mathbf{Z}$  coefficients.