

MATH 1572H SAMPLE MIDTERM PROBLEMS

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The midterm exam will cover the Sections 10.1 - 10.9, 11.1 - 11.3

1. Compute the following integrals. Note that some of these integrals are indefinite and some definite.

a) $\int_1^e \frac{\ln(x)^3}{x} dx$

b) $\int \sec^5(x)\tan^3(x)dx$

c) $\int_0^4 \sqrt{16-x^2}dx$

d) $\int \frac{x^5 + \sin(x)}{e^{x^2}} dx$

e) $\int \frac{x}{x^4 + 1} dx$

f) $\int \frac{1}{x^2 + 3x - 4} dx$

g) $\int \sin(4x)\cos(6x)dx$

2. Evaluate the following integrals

a) $\int \sec^3(x)dx$

b) $\int e^x \sin(x)dx$

3. Evaluate the following integrals

a) $\int \frac{\sqrt{49x^2 - 1}}{x} dx$

b) $\int \frac{x^2 - 29x + 5}{(x - 4)^2(x^2 + 3)} dx$

4. Using $n = 6$ and Simpson's rule approximate the value of the given integral.

$$\int_0^3 e^{x^2} dx$$

5. Use Pappus's Theorems to find the volume and the surface area of the torus (doughnut) generated by revolving a circle of radius r about a line in its plane at a distance R from its center, where $R > r$.