

MATH 1151 QUIZ-11 (15 minutes)

1. (5 points) Write $(\sqrt{3} - i)^6$ in the standard form $a+bi$.

Solution: Since $\sqrt{3} - i$ is in the fourth quadrant if you look at it you see that it's argument is $11\frac{\pi}{6}$ and it's length is 2. So that is we can write it in polar form as $2 * (\cos 11\frac{\pi}{6} + i \sin 11\frac{\pi}{6})$. So by using De Moivre's Theorem we see that sixth power of that number is equal to $2^6 * (\cos 6 * 11\frac{\pi}{6} + i \sin 6 * 11\frac{\pi}{6})$. So using the period we see that this is equal to $2^6 * (\cos \pi + i \sin \pi) = -2^6 = -64$ **Q.E.D.**

2.(5 points) Find the vertex, focus and directrix of the parabola $x^2 - 4x = 2y$, graph the equation.

Solution: This is equivalent to $x^2 - 4x + 4 = 2y + 4 = 2(y + 2)$ which is equal to $(x - 2)^2 = 2(y + 2)$. So vertex is $(2, -2)$ and since $4a = 2$ we have that $a = \frac{1}{2}$, so focus is $(2, -2 + \frac{1}{2} = (2, -\frac{3}{2})$ and directrix is $y = -2 - \frac{1}{2} = -\frac{5}{2}$, as you can see this is a parabola whose arms looks up, after that graphing is pretty easy. **Q.E.D.**