


Math and Climate Seminar IMA



Mathematics and Climate Research Network

Joint MCRN/IMA Math and Climate Seminar
 Tuesdays 11:15 – 12:05
 streaming video available at
www.ima.umn.edu

MCRN www.mathclimate.org

Glacial Cycles
 Last Week's News



<http://nsidc.org/arcticseaicenews/>

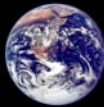
Glacial Cycles
 Last Week's News



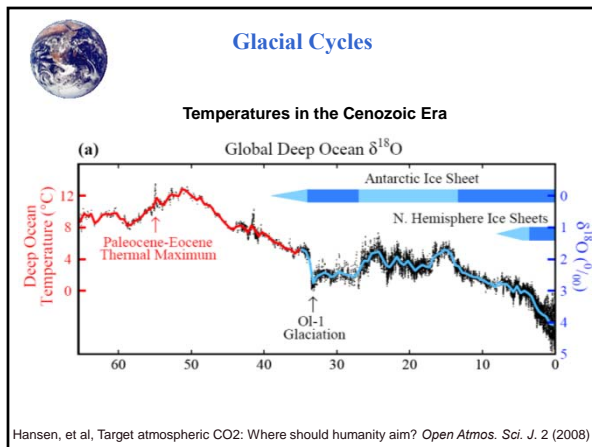
<http://www.nytimes.com/2012/09/19/science/earth/arctic-resources-exposed-by-warming-set-off-competition.html>

The Earth's Glacial Cycles

Richard McGehee

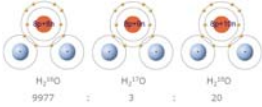


Seminar on the Mathematics of Climate
 IMA, MCRN, School of Mathematics
 September 25, 2012



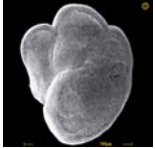
Glacial Cycles

¹⁸O as a Climate Proxy

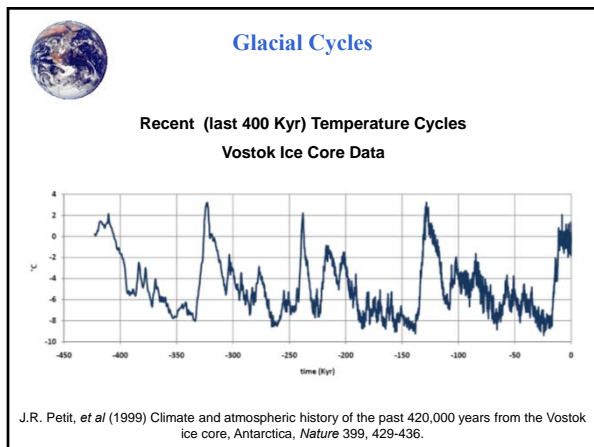
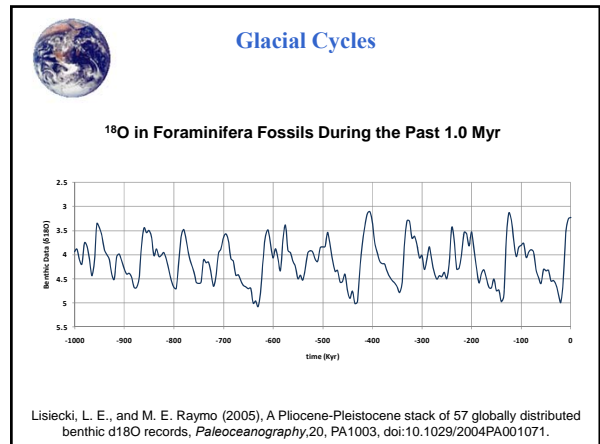
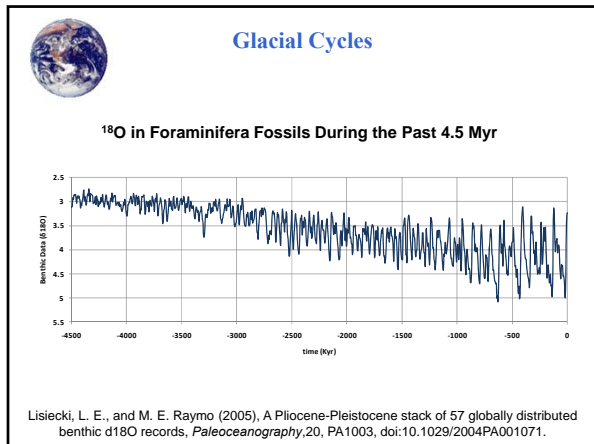


The isotope ¹⁶O preferentially evaporates from the ocean and is sequestered in glaciers, leaving the heavier isotope ¹⁸O more highly concentrated in the ocean. Thus oceanic concentration of the isotope ¹⁸O is higher during glacial periods.

Foraminifera absorb more ¹⁸O into their skeletons when the water temperature is lower and when more ¹⁸O is in the water.



Thus higher concentrations of ¹⁸O in foraminifera fossils indicate lower ocean temperatures and higher glacier volume.



Glacial Cycles

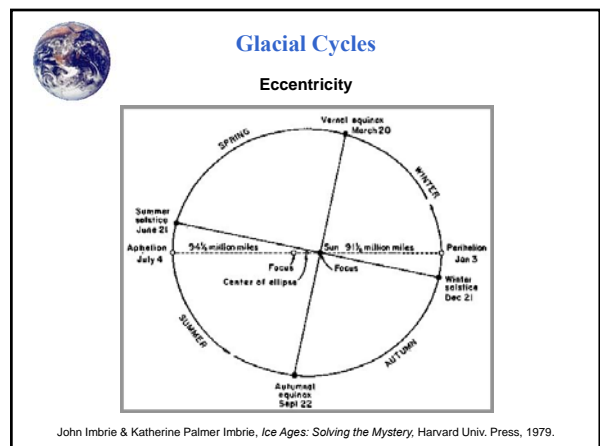
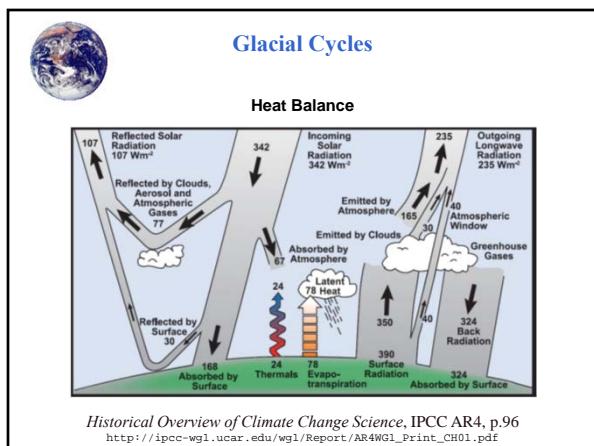
What Causes Glacial Cycles?

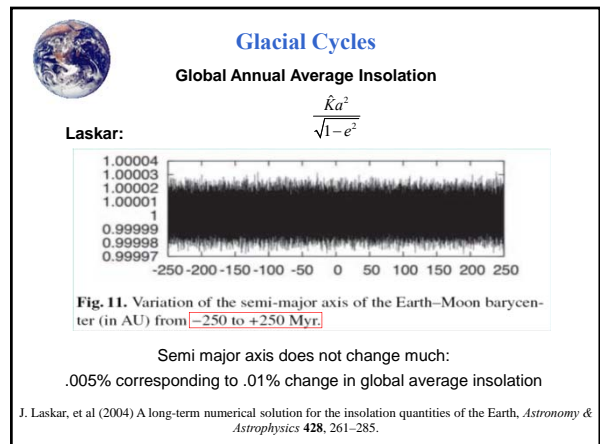
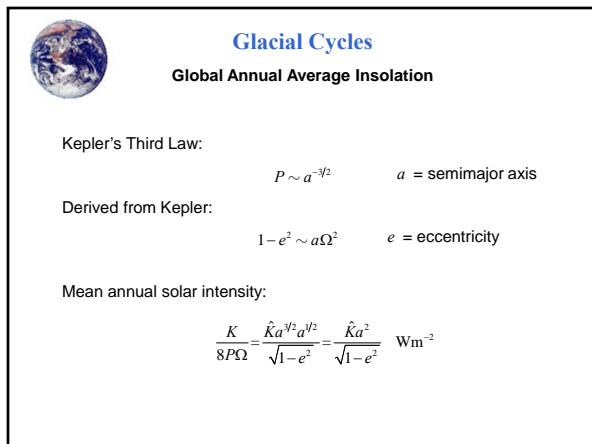
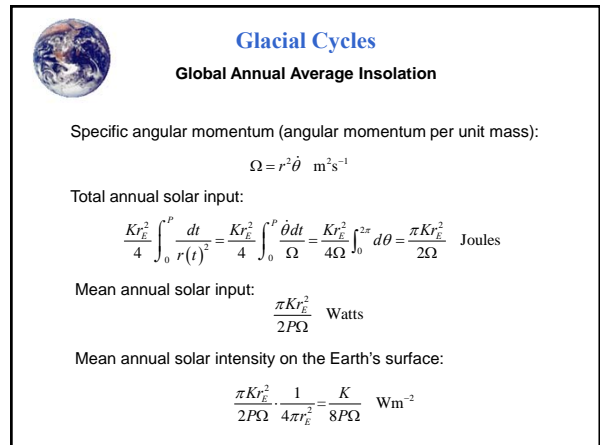
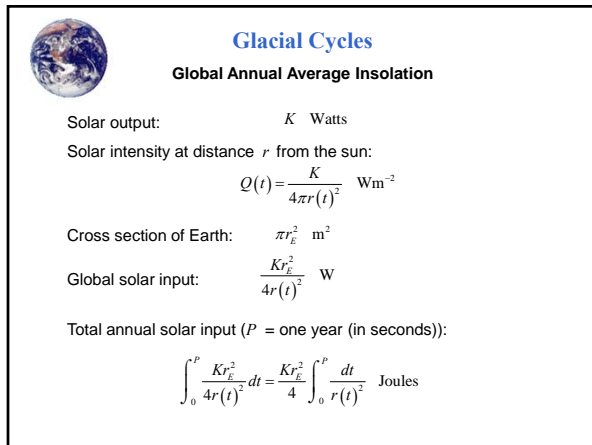
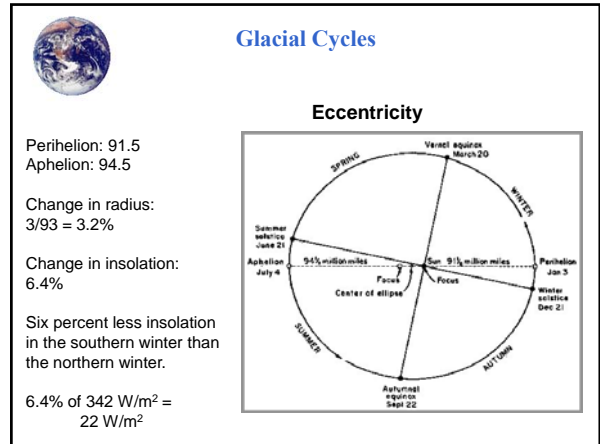
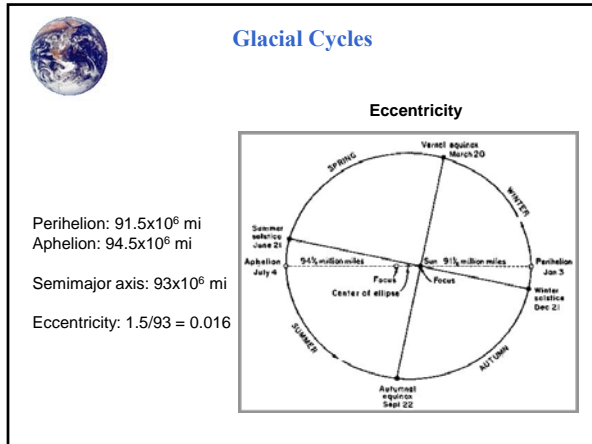
Widely Accepted Hypothesis

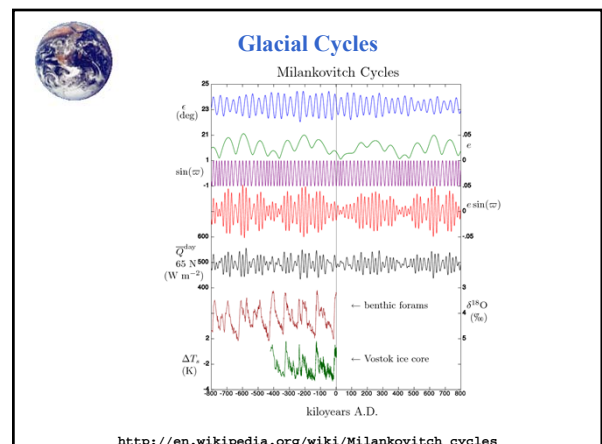
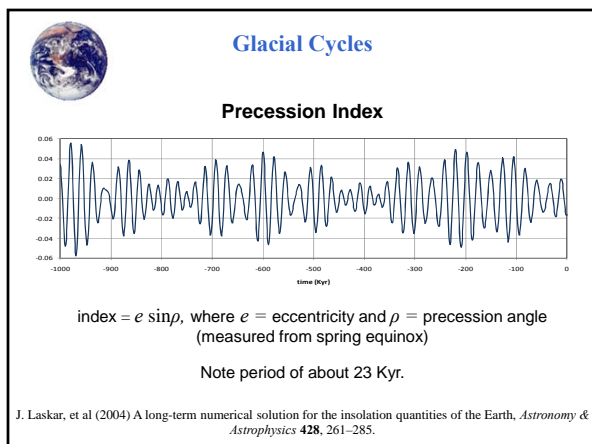
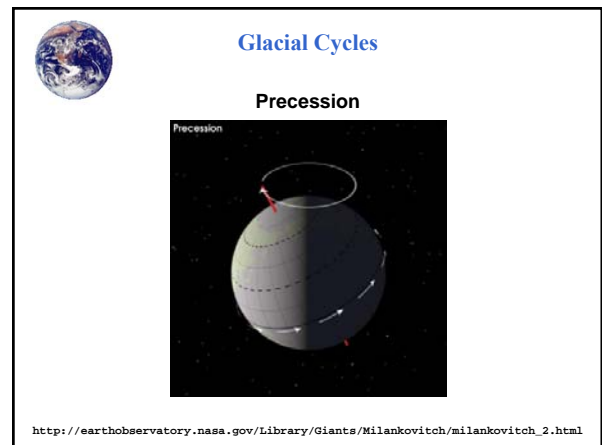
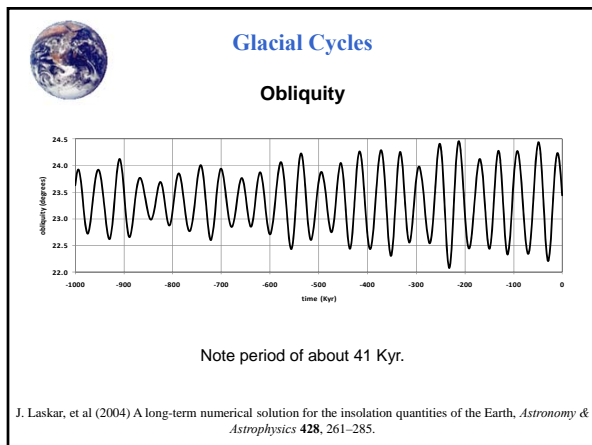
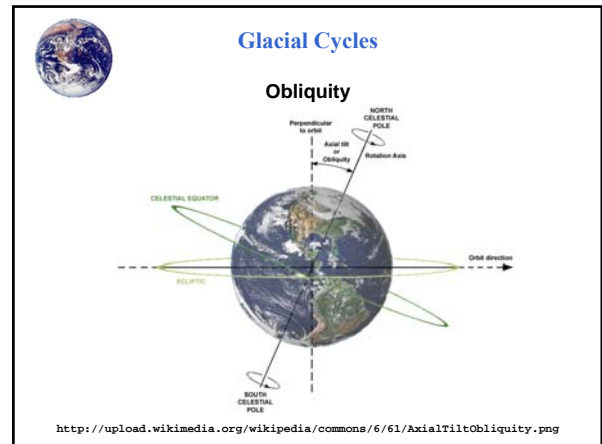
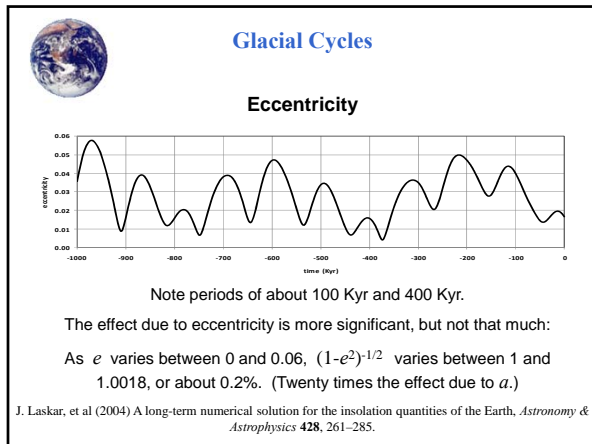
The glacial cycles are driven by the variations in the Earth's orbit (Milankovitch Cycles), causing a variation in incoming solar radiation (insolation).

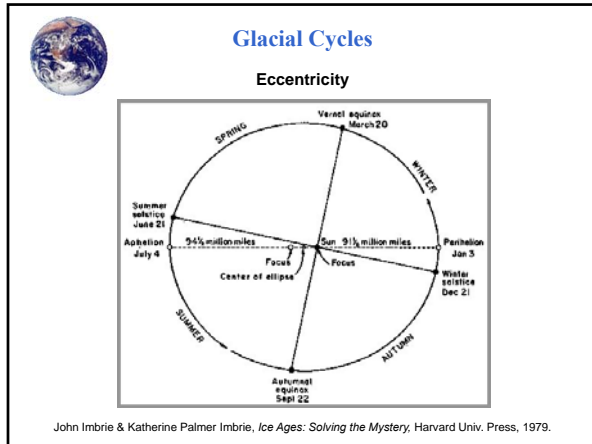
This hypothesis is widely accepted, but also widely regarded as insufficient to explain the observations.

The additional hypothesis is that there are feedback mechanisms that amplify the Milankovitch cycles. What these feedbacks are and how they work are not fully understood.









Glacial Cycles

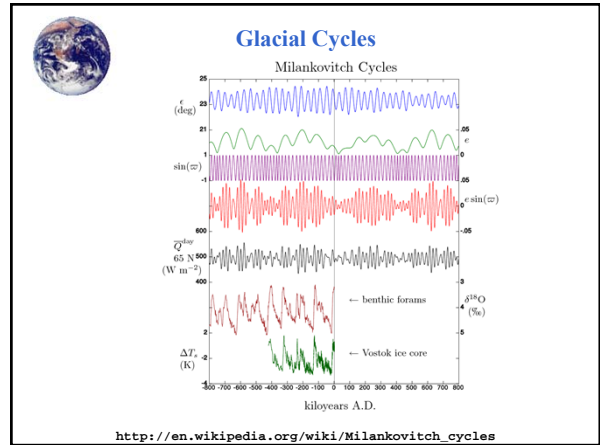
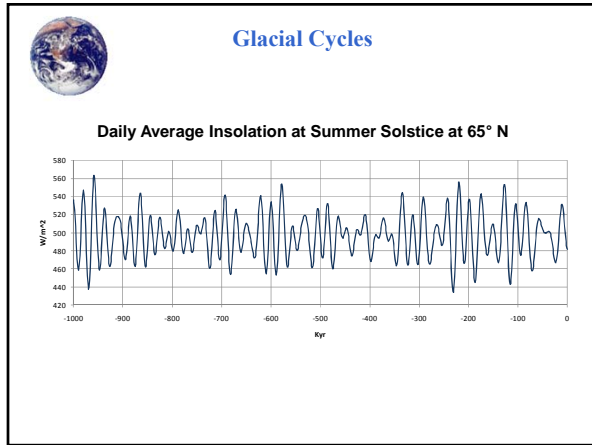
Daily Average Insolation at Summer Solstice at 65° N

Insolation at a point on the Earth's surface

$$I(\beta, \rho, r, \theta, \phi, \gamma) = \frac{K}{4\pi r^2} [-\cos \phi (\cos \beta \cos(\theta - \rho) \cos \gamma + \sin(\theta - \rho) \sin \gamma) - \sin \phi \sin \beta \cos(\theta - \rho)]$$

(ϕ, γ) = (latitude, longitude)
 (r, θ) = position of Earth in orbital plane
 β = obliquity angle
 ρ = precession angle

Daily average insolation at latitude ϕ at summer solstice

$$\bar{I}(e, \beta, \rho', \phi) = Q \frac{(1 - e \sin \rho')^2}{(1 - e^2)^2} \frac{1}{2\pi} \int_0^{2\pi} [\cos \phi \cos \beta \cos \gamma + \sin \phi \sin \beta] d\gamma$$


Glacial Cycles

Who was Milankovitch?

Milutin Milankovitch
1879-1958

Milutin Milankovitch was a Serbian mathematician and professor at the University of Belgrade.

In 1920 he published his seminal work on the relation between insolation and the Earth's orbital parameters.

In 1941 he published a book explaining his entire theory.

His work was not fully accepted until 1976.

Glacial Cycles

What happened in 1976?

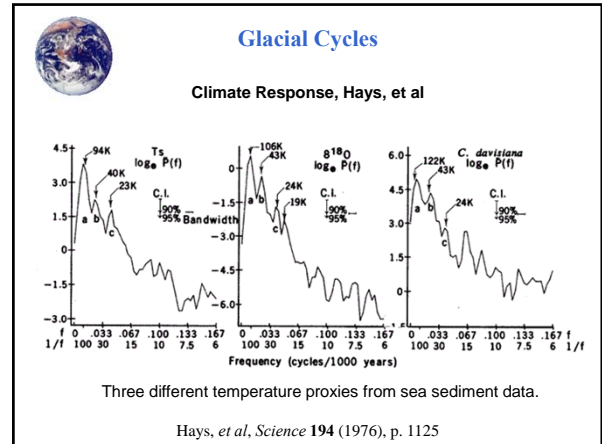
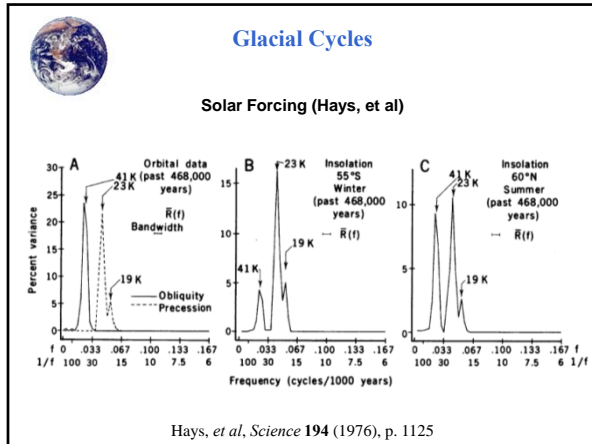
James D. Hays

Hays, Imbrie, and Shackleton, "Variations in the Earth's Orbit: Pacemaker of the Ice Ages," *Science* 194, 10 December 1976.

John Imbrie

"It is concluded that changes in the earth's orbital geometry are the fundamental cause of the succession of Quaternary ice ages."

Nicholas Shackleton



Glacial Cycles

Hays, et al, Summary

- 1) Three indices of global climate have been monitored in the record of the past 450,000 years in Southern Hemisphere ocean-floor sediments.
- 2) ... climatic variance of these records is concentrated in three discrete spectral peaks at periods of 23,000, 42,000, and approximately 100,000 years. These peaks correspond to the dominant periods of the earth's solar orbit, and contain respectively about 10, 25, and 50 percent of the climatic variance.

Hays, et al, *Science* 194 (1976), p. 1125

Glacial Cycles

Hays, et al, Summary

- 3) The 42,000-year climatic component has the same period as variations in the obliquity of the earth's axis and retains a constant phase relationship with it.
- 4) The 23,000-year portion of the variance displays the same periods (about 23,000 and 19,000 years) as the quasiperiodic precession index.
- 5) The dominant, 100,000-year climatic component has an average period close to, and is in phase with, orbital eccentricity. Unlike the correlations between climate and the higher-frequency orbital variations (which can be explained on the assumption that the climate system responds linearly to orbital forcing), **an explanation of the correlation between climate and eccentricity probably requires an assumption of nonlinearity.**

Hays, et al, *Science* 194 (1976), p. 1125

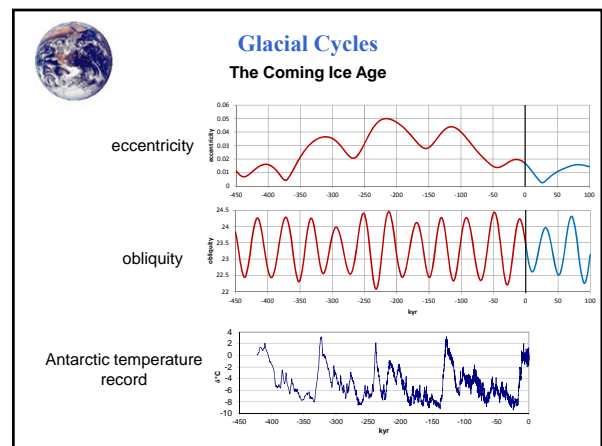
Glacial Cycles

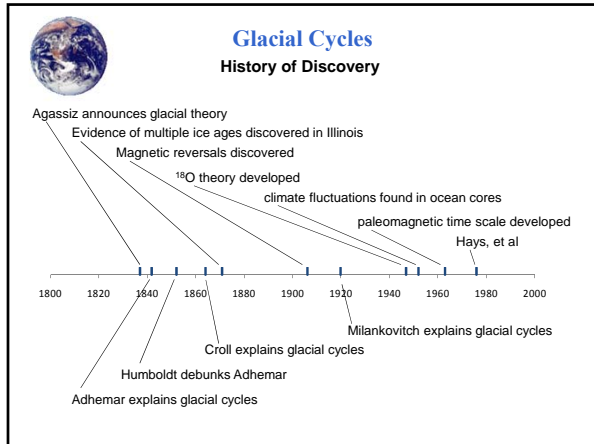
Hays, et al, Summary

- 6) It is concluded that changes in the earth's orbital geometry are the fundamental cause of the succession of Quaternary ice ages.
- 7) A model of future climate based on the observed orbital-climate relationships, **but ignoring anthropogenic effects**, predicts that the long-term trend over the next seven thousand years is toward **extensive Northern Hemisphere glaciation**.

*Quoted by George Will, Washington Post, February 5, 2009

Hays, et al, *Science* 194 (1976), p. 1125





Glacial Cycles

Next Week

Glacial Cycles: Theory Since 1976.