MATH 1001, Fair Division Quiz, Spring, 2003
Remember, there will be little or no partial credit given on questions in this quiz.

TRUE/FALSE (2 points each) Answer the following questions by writing a T or F in the blank.
___ T__ 1. If I split a cake with somebody using the "You Cut/I Choose" method, it is possible that my fair share will be worth more than $50 \%$ to me.

Look in your book: the chooser might get a piece worth more than $50 \%$ to her.
___ T __ 2. Whether or not my piece of a cake is a a fair share only depends on my perceptions, and not what any other player thinks about my piece.
$\qquad$ 3. In the Lone Chooser method, with 3 players, the cake will be split into 6 pieces before the Chooser actually chooses anything.
$\qquad$ 4. 10 players are splitting a cake using the Last Diminisher method, and it is $P_{4}$ 's turn during the first round. If $P_{4}$ thinks the current piece is worth exactly $10 \%$, then she will choose to play, cut off a slice, and claim the new C-piece. (Think carefully here!)

If $P_{4}$ chooses to play, he has to cut off part of the C-piece, which would make it worth less than $10 \%$, so it wouldn't be a fair share anymore.
$\qquad$ 5. If there are four players sharing a cake, then a "fair share" for a player is any piece that she thinks is worth at least $33 \frac{1}{3} \%$ of the total cake.
$100 \%$ divided by 4 players is $25 \%$.
5. My son and two nephews split a cupcake using the Lone Divider method. The Divider cuts three pieces, $s_{1}, s_{2}$, and $s_{3}$. The following table shows how much each piece is worth to each player.

|  | $s_{1}$ | $s_{2}$ | $s_{3}$ |
| :---: | :---: | :---: | :---: |
| $D$ | $33 \frac{1}{3} \%$ | $33 \frac{1}{3} \%$ | $33 \frac{1}{3} \%$ |
| $C_{1}$ | $20 \%$ | $20 \%$ | $60 \%$ |
| $C_{2}$ | $20 \%$ | $40 \%$ | $40 \%$ |

Write down $C_{1}$ 's bid and $C_{2}$ 's bid. (2 Points)

$$
\begin{array}{cc}
C_{1} & :\left\{s_{3}\right\} \\
C_{2} & :\left\{s_{2}, s_{3}\right\}
\end{array}
$$

Describe a fair division of the cupcake. (3 Points)
$D$ gets $s_{1}$
$C_{1}$ gets $s_{3}$
$C_{2}$ gets $s_{2}$

