MTH G375: TOPICS IN TOPOLOGY: OPERADS PROBLEM SET 3, DUE APRIL 15, 2004

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I encourage you to cooperate with each other on the homeworks. This time you may not turn in your homework late, as I will leave the morning April 16 for Minnesota for good!

Problem 1. Identify the cohomological complex for an algebra over the associative operad as the Hochschild complex, see your notes, Markl-Shnider-Stasheff, or Ginzburg-Kapranov (dualize 4.2). You may download GK's paper for free from http://projecteuclid.org:80/Dienst/UI/1.0/Summarize/euclid.dmj/1077286744?abstract= till March 31 only!

Problem 2. Identify the dg dual D(Ass) (see your notes or MSS or GK) with the planar tree complex.

Problem 3. Prove that the homology of the (nonframed) little (two-dim) disks operad is the operad describing G-algebras. A G-algebra is the same as a BV-algebra, but without the BV operator.

Problem 4 (Essay). In which sense does the free loop space LM of a manifold constitute a TCFT in genus zero?

Problem 5 (After Givental. Perhaps, related to mirror symmetry). Why do we see ourselves in the mirror with left changed to right, but not upside down?