## Math 8201Homework 10Date due: November 20, 2017. There will be a quiz on this date.

Hand in only the starred questions.

Section 7.1 1, 6, 7, 9, 10<sup>\*</sup>, 11, 13, 14<sup>\*</sup>, 15, 16<sup>\*</sup>, 21, 24, 28<sup>\*</sup>, 30 There are many good questions in the exercises at the end of this section.

- II. Find a ring R and elements a, b, c all distinct from 0 such that  $a \cdot b = a \cdot c$  and yet  $b \neq c$ .
- JJ. Show that the quaternions z for which  $z^2 + 1 = 0$  are precisely those which may be written z = bi + cj + dk with  $b^2 + c^2 + d^2 = 1$ . [Hint: you may want to show as a first step that if z satisfies the equation then  $z = \pm \overline{z}$ , and then go on to show that in fact  $z = -\overline{z}$ . Now continue.]

Section 7.2 2, 7\*, 8